



## Double Fano resonances in a planar pseudo-dolmen structure



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### ABSTRACT

The transmittance properties of a planar pseudo-dolmen plasmonic structure were investigated using finite element method. Numerical results show that double Fano resonances are caused by the strong electric field coupling between bright and dark modes. The dark plasmon resonances are highly dependent on the structure parameters of the pseudo-dolmen structure. The Fano resonances in the pseudo-dolmen structure are also sensitive to small changes in the refractive index of the surrounding media. This characteristic could be effectively used to fabricate bi-wavelength sensors.

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### 1. Introduction

In 1961, Ugo Fano described the asymmetric spectral lineshape with the expression of the form  $I \propto (F\gamma + \omega - \omega_0)^2 / [(\omega - \omega_0)^2 + \gamma^2]$ , where  $\omega_0$  and  $\gamma$  are standard parameters that denote the position and width of the resonance, respectively;  $F$  is the so-called Fano parameter, which describe the degree of asymmetry [1]. Recently, Fano resonances in a plasmonic system have been extensively studied because of their potential applications in chemical and biological sensors [2–4], slow light [5,6], surface enhanced Raman scattering [7,8], and plasmon rulers [9].

Fano resonance is caused by hybridization between a narrow discrete resonance (dark mode) and a broad continuum state (bright mode) [10]. A bright mode is excited by incident light, and a dark mode is indirectly excited through coupling with the bright mode [11]. Tuning Fano resonances is important to modify optical responses by changing the asymmetric line shape and the localized electromagnetic field distribution in the dark mode. Many researchers have focused on Fano resonances in various plasmonic systems, such as dolmen nanostructures [6,12,13], nanoparticle clusters [14–16], metal-nanoshells [17], metal dimers [18,19], and ring/disk cavities [20].

Many efforts were spent to make 2D plasmonic material, such as the highly doped 2D MoS<sub>2</sub> and molybdenum oxide nanoflakes, with resonant wavelengths in near IR and visible regions [21,22]. Despite considerable efforts to achieve single Fano resonance in dif-

ferent types of plasmonic structures, several designs have achieved multiple Fano resonances; these designs include metal-dielectric core-shell nanoparticle oligomers (MDCs) [23], dimer/monomer slab and ring-near-disk cavity (RNDC) [24], asymmetrically split rings (ASR) [25], and double symmetrical U-shaped split-ring resonators (SRRs) with a nanorod between the two SRRs (SRRs/Rod) [26]. Dark modes are generated in plasmonic systems with different designs to obtain multiple Fano resonances. In the MDCS structure, an additional dark mode is provided by adding dielectric to the heptamer structure [23]. In dimer/monomer slab and RNDC structures, multiple Fano resonances arise for the same structures with larger dimensions [24]. In the ASR structure, double dark modes are generated by introducing structural symmetry breaking [25]. In the SRR/Rod structure, an additional dark mode is provided by changing the coupling distance between the nanorod and the double symmetrical U-shaped split-ring resonators [26]. In general, the double Fano resonances are realized in a relatively complex structure for inducing one more dark mode.

In this paper, we demonstrate that the occurrence of two Fano resonances in a planar pseudo-dolmen structure (PDS) is caused by the electric field coupling between nanorods with different lengths. Numerical calculations show that the Fano resonances are strongly dependent on the length of nanorods in the PDS structure and on the separation between adjacent nanorods. Two dark modes can be tuned independently by varying the length of nanorods as well as the separation between them. And they are sensitive to the refractive index changes of the surrounding environment. This characteristic could be effectively used to fabricate double-wavelength sensors.

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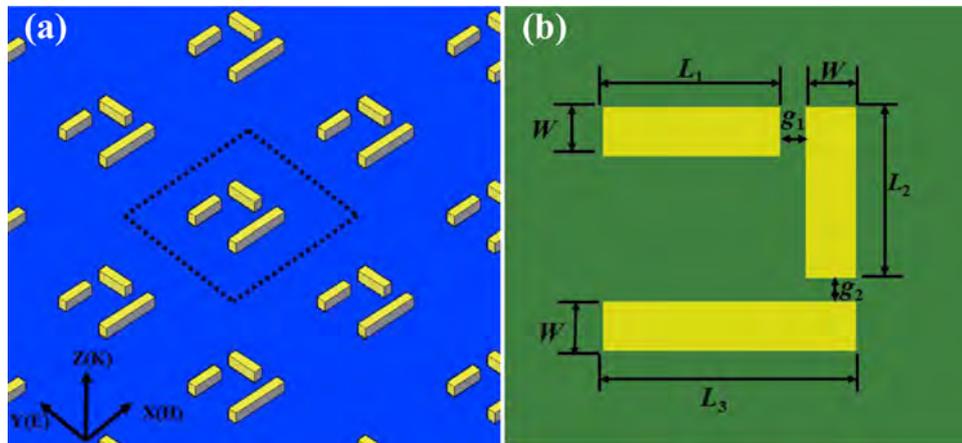


Fig. 1. (a) Pseudo-dolmen structure arrays and (b) the unit cell with geometrical parameters.

### 2. Structure and computational method

Fig. 1 presents the periodic PDS arrays and their structural parameters. The PDS consists of three metallic nanorods arranged perpendicularly to each other. The incident light normally illuminates the structure along the  $-z$  direction with polarization along the  $y$  direction. The lengths of nanorods 1–3 are defined as  $L_1$ ,  $L_2$ , and  $L_3$ , respectively. Fig. 1 shows that the gap between the nanorods is  $g_1 = g_2 = 10$  nm, and the period in the  $x$  and  $y$  directions is 200 nm. The three metallic nanorods also demonstrate a fixed square cross section of  $20 \text{ nm} \times 20 \text{ nm}$ .

The transmittance spectra of the PDS arrays are derived using the three-dimensional finite element method with the software COMSOL Multiphysics simulation. The stationary frequency solver is applied for this static situation. Periodic boundary conditions are imposed on four sides of the unit cell to simulate the infinite 2D array. The refractive index of the surrounding media is 1, and the selected metallic element is gold, whose frequency-dependent permittivities are obtained from Ref. [27].

### 3. Results and discussion

Fig. 2(a) shows the transmittance spectrum of the PDS with  $L_1 = L_2 = 70$  nm,  $L_3 = 100$  nm, and  $g_1 = g_2 = 10$  nm. Three resonant wavelengths appear in the spectra at  $\lambda = 642$  nm, 702 nm, and 824 nm. For comparison, the longitudinal modes of these nanorods with similar parameters to those in Fig. 2(a) are calculated. Fig. 2(b) and (c) indicate that the longitudinal resonant modes for nanorods 1 (or 2) and 3 are  $\lambda = 660$  nm and 770 nm, respectively.

The electric field spatial distribution in the resonant modes in Fig. 2(a) is calculated to elucidate the resonance characterizes of the PDS. Fig. 3(a) indicates that the electric fields are mainly distributed at the two ends of nanorod 2 at  $\lambda = 642$  nm. This mode is mainly due to the dipole electric oscillation on nanorod 2. This mode can be excited under the  $y$  direction polarization incidence and is called the bright mode (mode B, resonant wavelength  $\lambda_B$ ). Fig. 3(b) shows that strong electric fields appear at the two ends of nanorods 1 and 2 at  $\lambda = 702$  nm. Specifically, strong electric fields exist between nanorods 1 and 2. The incident light with  $y$  direction polarization excites electron oscillations in the  $x$  direction on nanorod 1. This mode is a dark mode and denoted as mode  $D_1$  with the resonant wavelength  $\lambda_{D_1}$ . Fig. 3(c) demonstrates that the strong electric fields appear at the two ends of nanorods 2 and 3 at  $\lambda = 824$  nm. In particular, strong electric fields exist between nanorods 2 and 3. The incident light with  $y$  direction polarization excites electron oscillation in the  $x$  direction on nanorod 3. This mode is a dark mode and denoted as mode  $D_2$  with the resonant

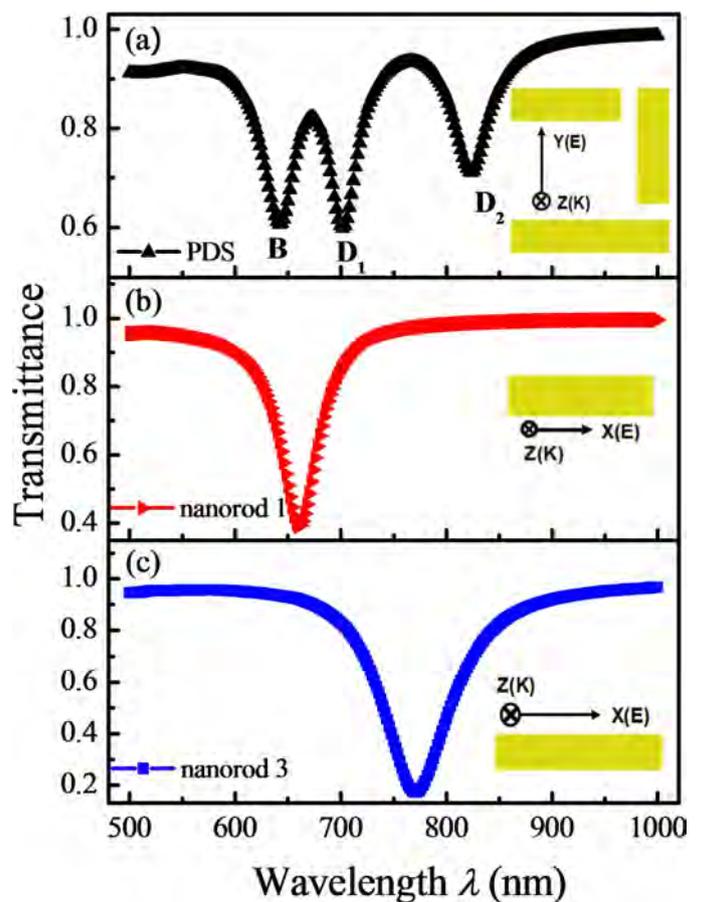


Fig. 2. Transmittance spectra of (a) PDS with  $E_y$  polarization, (b) nanorod 1 with longitudinal polarization, and (c) nanorod 3 with longitudinal polarization.

wavelength  $\lambda_{D_2}$ . From these results, one bright mode (mode B) and two dark modes (modes  $D_1$  and  $D_2$ ) can be excited for the PDS. The well-separated dark modes in the transmission spectrum confirm that the PDS is a simple structure that can achieve double Fano resonances.

The dimensions of the PDS are systematically varied to investigate the effects of structural parameters on the Fano resonances. First,  $L_1$  is varied to study the effect of the length of nanorod 1 on the Fano resonances of the PDS as shown in Fig. 4(a). The gap between adjacent nanorods is set at 10 nm. Fig. 4(a) shows that modes B and  $D_1$  red shift with the extension of  $L_1$ , and mode  $D_2$

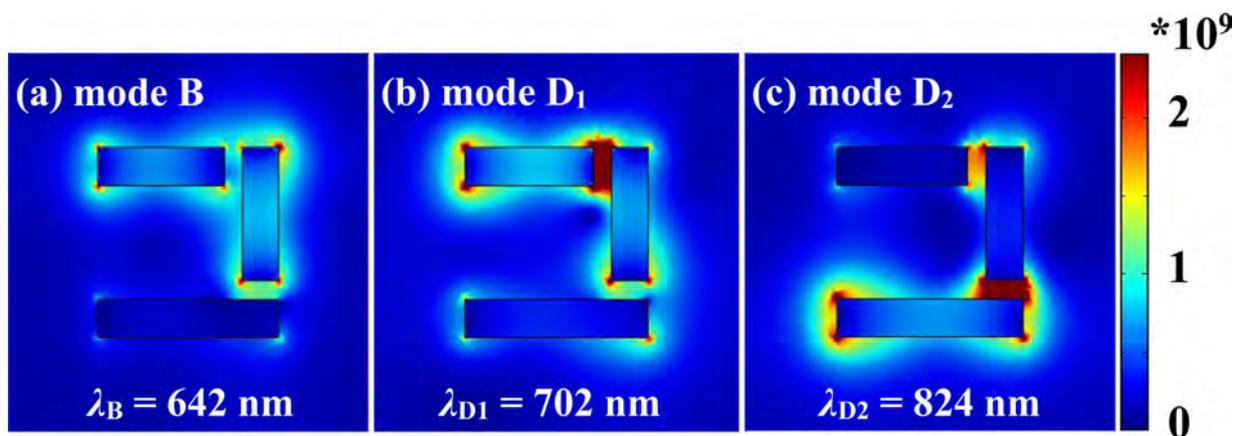


Fig. 3. Electric field distributions of the PDS at different modes (a) mode B, (b) mode D<sub>1</sub>, and (c) mode D<sub>2</sub>.

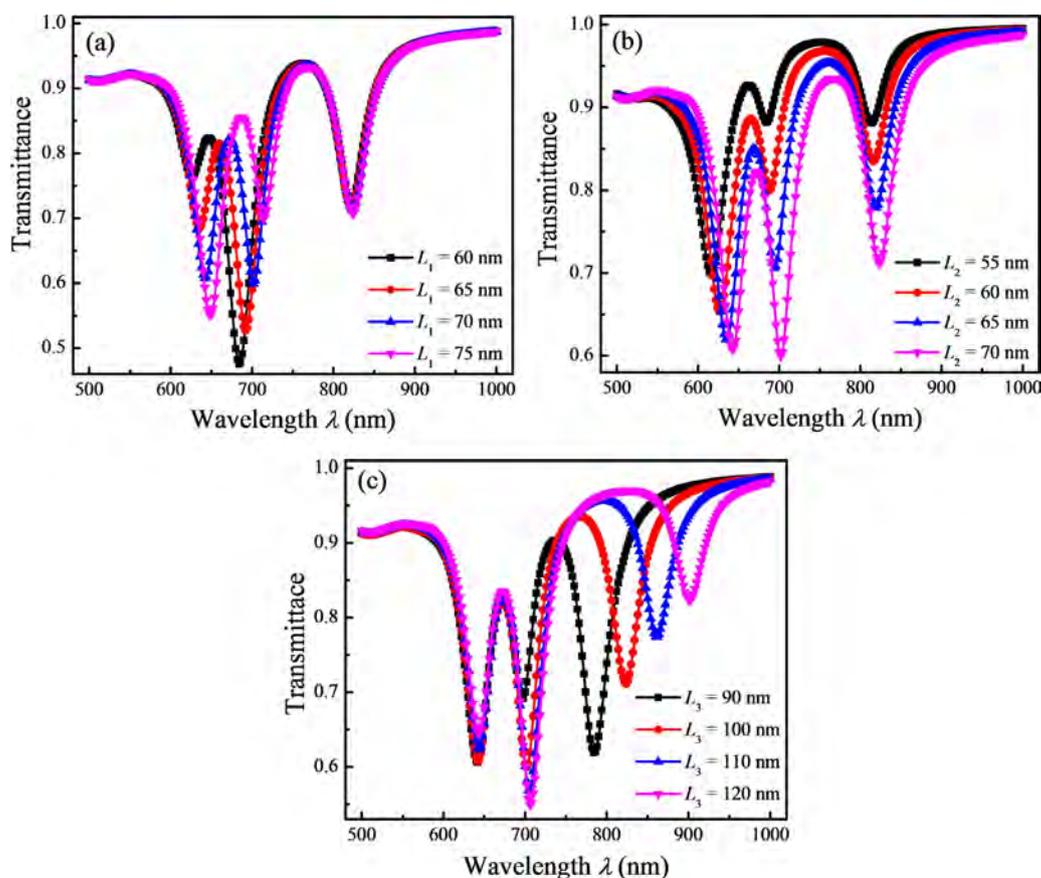


Fig. 4. Transmittance spectra of the PDS with different nanorod lengths: (a) different  $L_1$ ; (b) different  $L_2$ ; (c) different  $L_3$ .

does not evidently shift. Fig. 3(a) presents a weak electric field coupling between nanorods 1 and 2 of mode B. The increasing length of nanorod 1 extends the electron oscillations of mode B, causing the mode to red shift. The increment in  $L_1$  also extends the electron oscillations of mode D<sub>1</sub> and results in the red shift of the mode. By contrast, the increment in  $L_1$  does not affect mode D<sub>2</sub> because the mode is mainly caused by the electron oscillations on nanorods 2 and 3. As a result, mode D<sub>1</sub> can be tuned independently by varying the length of  $L_1$ . Fig. 4(b) further shows the transmittance spectra of the PDS with different  $L_2$  values and a fixed gap of 10 nm. All resonant modes red shift with increasing  $L_2$  values because of the increasing electron oscillation length in the resonant modes. Fig. 4(c) indicates that mode D<sub>2</sub> red shifts with the extension of  $L_3$ ,

and mode B and D<sub>1</sub> do not evidently shift. The increment of  $L_3$  only increases the electron oscillation length of mode D<sub>2</sub>. Thus, mode D<sub>2</sub> can also be tuned independently by varying the length of  $L_3$ .

The gaps  $g_1$  and  $g_2$  are varied with fixed  $L_1 = L_2 = 70$  nm and  $L_3 = 100$  nm to investigate their effects on Fano resonances of the PDS. Fig. 5(a) shows the transmittance spectra of the PDS with  $g_1 = 10$  nm, 15 nm, 20 nm, and 25 nm and  $g_2 = 10$  nm. The increase in  $g_1$  weakens the coupling between nanorods 1 and 2; The weakened coupling decreases the electron oscillation length of mode D<sub>1</sub> and leads to the evident blue shift of  $\lambda_{D1}$ . Fig. 5(b) presents the transmittance spectra of the PDS with  $g_2 = 10$  nm, 15 nm, 20 nm, and 25 nm and fixed  $g_1 = 10$  nm. With increasing  $g_2$ , mode D<sub>2</sub> blue

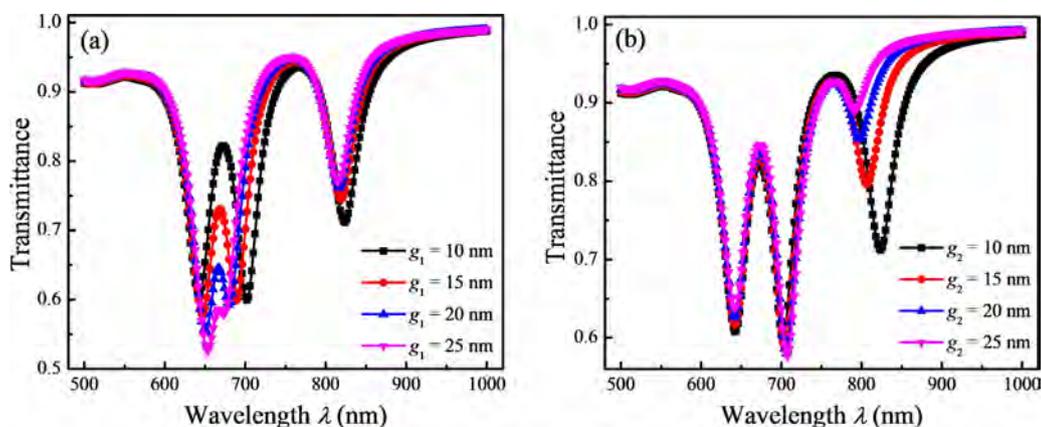


Fig. 5. Transmittance spectra of the PDS with different gaps: (a) different  $g_1$ ; (b) different  $g_2$ .

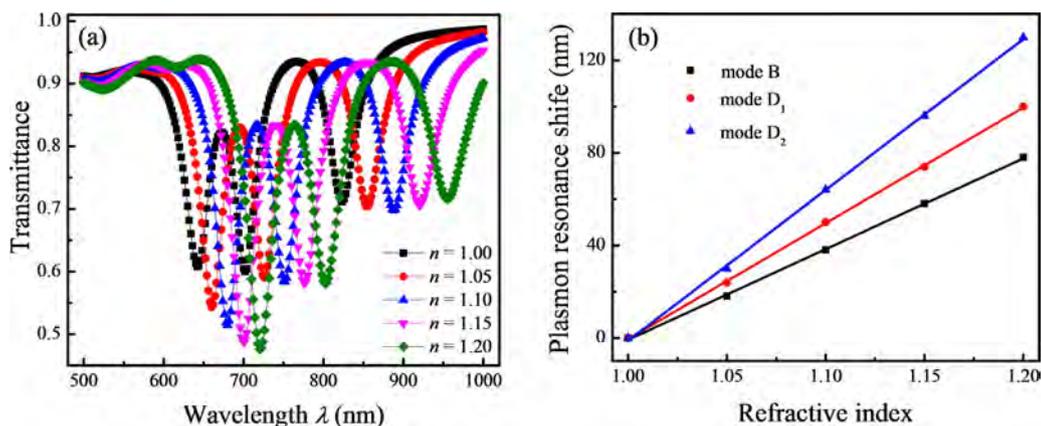


Fig. 6. (a) Transmittance spectra of PDS with the environments of different refractive indexes; (b) the resonance wavelengths as a function of refractive index.

shifts because of the decreasing coupling strength. But modes B and  $D_1$  are not affected.

The value of  $n$  is increased from 1 to 1.2 with fixed  $L_1 = L_2 = 70$  nm,  $L_3 = 100$  nm, and  $g_1 = g_2 = 10$  nm to investigate how the dielectric constants of the surrounding media affect the sensing performance. Fig. 6(a) shows that all resonance modes red shift with increasing refractive index of the dielectric environment. Fig. 6(b) also presents that the plasmon resonance shifts with increasing of the refractive index of the surrounding media. The lines in Fig. 6(b) represent the linear fittings. The resonant wavelengths of the three modes show a linear relationship to  $n$ . The calculated sensitivities are  $S_B = 378$  nm/RIU,  $S_{D_1} = 492$  nm/RIU, and  $S_{D_2} = 630$  nm/RIU.

A high figure of merit (FOM) is preferred than the index shift of plasmon resonance for sensing applications because of its narrow width. FOM is used to directly compare the overall performance of sensors by using the following formula  $FOM = m/fwhm$ , where  $fwhm$  is the full width at half the maximum centered at the resonance wavelength  $\lambda$ , and  $m$  is the linear regression slope for the refractive index dependence (i.e., spectral shifts per refractive index) [28]. The  $fwhm$  values of modes B,  $D_1$ , and  $D_2$  are  $fwhm_B = 0.0743$  eV (30 nm),  $fwhm_{D_1} = 0.0561$  eV (28 nm), and  $fwhm_{D_2} = 0.0499$  eV (34 nm), respectively; their corresponding  $m$  values are  $m_B = 1.053$  eV/RIU,  $m_{D_1} = 1.103$  eV/RIU, and  $m_{D_2} = 1.03$  eV/RIU, respectively. The calculated FOMs of modes B,  $D_1$ , and  $D_2$  are  $FOM_B = 14.73$ ,  $FOM_{D_1} = 20.44$ , and  $FOM_{D_2} = 21.22$ , respectively. These FOMs are stronger than those of the individual plasmonic particles [24]. The high FOM based on plasmonic mode coupling may be useful for applications requiring high-sensitivity detection.

#### 4. Conclusions

In this study, a planar PDS is proposed to create two dark modes and then to generate double Fano resonances. Dark mode  $D_1$  is introduced by the coupling effect between nanorods 1 and 2, and dark mode  $D_2$  is introduced by the coupling between nanorods 2 and 3. The dark modes are highly dependent on the structural parameters of the PDS and can be tuned independently. The influences of the refractive index on the bright and dark modes are investigated for sensing applications. The results show the potential applications of the PDS in single- or double-wavelength sensing.

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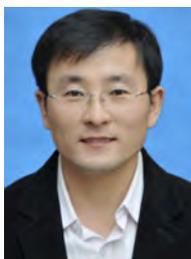
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